

# PERFORMANCE EVALUATION OF SECURITY WHEN USING ARTIFICIAL NOISE FOR ONE-WAY FULL-DUPLEX RELAY NETWORKS

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## ABSTRACT

In this paper, we are presenting a method to improve physical layer security (PLS) in wireless communication networks. Specifically, we would like to propose a one-way full-duplex (OWFD) relay network model with artificial noise (AN). The model consists of five nodes (source node, destination node, relay node, eavesdropping node, jamming node). To evaluate the security performance of the model, we analyzed key performance metrics such as the secrecy outage probability (SOP) and the system's secrecy throughput (STP) through deriving closed-form expressions for SOP and STP. Simulation results verify the proposed expressions using the Monte-Carlo method. The findings of this study demonstrated a significant improvement in security performance compared to previous researches. Additionally, the proposed model has highlighted the feasibility of implementing PLS techniques in OWFD relay networks.

**Keywords:** Physical layer security, Secrecy outage probability, Secure throughput, Artificial noise, One-way full-duplex.

## 1. INTRODUCTION

Wireless networks, with their widespread applications, have become an indispensable part of our daily lives. These networks have been increasingly demanding more spectral resources to accommodate the growing number of users [1]. Full-duplex (FD) technology allows simultaneous transmission and reception on a single time-frequency channel, promising nearly to double the spectral efficiency compared to half-duplex (HD) systems [2-5]. In FD techniques, signals are transmitted and received on the same frequency and at the same time [6]. One of the growing concerns in wireless communication is the security of transmitted signals. Due to the open nature of wireless networks, they are inherently insecure [7]. The simplicity of accessing the wireless medium made communications easier to be eavesdropped on over this medium [8]. The artificial noise (AN) approach - proposed by Goel and Negi [9, 10] is a technique to ensure absolute secure communication between legitimate nodes. The authors demonstrated that perfect security could be achieved when the channel of the eavesdropper was noisier than the channel of the legitimate receiver. AN is added to the null space of the legitimate receiver's channel so that it deteriorates the signal reception of the eavesdroppers without harming the communications of the legitimate receiver [11].

### 1.1. Related works

In [12], the author analyzed and evaluated the trade-off between system reliability and security, using a Rayleigh fading channel, FD communication, and the DF protocol at the relay node, PLS is achieved by introducing AN to the eavesdropping node. In [13], the author evaluated the SOP and STP of the system, considering a Rayleigh fading channel, the DF protocol, and FD at the relay node, PLS is implemented by harvesting energy at the system's relay node. The research group also investigated, analyzed, and evaluated the SOP and interception probability (IP) of the system, where a Rayleigh fading channel was used in the model with the amplify-and-forward (AF) protocol and HD operation at

the relay node [14]. A system consisting of five nodes, including one node acting as a signal reflector for the source node's transmission, was studied using a Rayleigh fading channel, HD operation, and the DF protocol at the relay node, the model examines the OP and secure energy efficiency performance, enhancing system security through an intelligent reflecting surface (IRS) [15]. In [16], the research group analyzed and evaluated the OP and IP of the system, using a Nakagami-m fading channel, the system does not employ FD devices, and PLS is achieved by utilizing an IRS for signal forwarding, since the signal is directly transmitted, neither the AF nor DF protocol is used. Notably, in [17], the author investigated the hardware of reconfigurable intelligent surfaces (RIS) to optimize PLS, introduced corresponding scenarios, and studied system models that do not include FD or relay devices. The author also discussed potential future research directions and challenges in RIS-assisted PLS communication.

From the above studies, we have also identified open issues for future research, such as introducing additional jamming devices into the system, enabling full-duplex operation at the source, relay, and legitimate receiver, adding a direct link from the source to both the legitimate receiver and the eavesdropper in the research model, modifying the channel model, and changing the relay node protocol.

## 1.2. Motivation

Although studies [12-17] analyzed and evaluated the trade-off between reliability and security, SOP, and STP for half-duplex and full-duplex models with relay nodes, jamming from the source node, and Rayleigh fading and Nakagami-m channels, they have not yet addressed the destination node in the system or artificial jamming from external nodes. Additionally, the direct signal transmission path from the source node to the destination node has not been investigated for this system.

This paper minimizes the signal-to-noise ratio (SNR) at the eavesdropping node by introducing interference from an external node and the destination node to enhance security and significantly improve the secrecy performance of the OWFD relay network. On the other hand, FD at the legitimate receiving node helps save bandwidth and protect useful information during signal transmission.

The main contributions of this paper include the following:

- Generate AN to enhance information security and apply FD to save bandwidth for the OWFD relay network.
- Propose closed-form and accurate expressions for SOP and STP for analyzing the performance of the OWFD relay network.
- Effectively demonstrate the role of AN generators and their significant impact on system performance in preventing eavesdropping.
- Conduct Monte Carlo simulations to validate the accuracy of the SOP and STP expressions.

## 1.3. Organization

This paper is structured into six sections as follows. The next section presents the system model under consideration. Section 3 analyzes and provides details on the expressions for secrecy outage probability (SOP) and secure throughput (STP). Section 4 presents the results and discussions. Section 5 provides the conclusion. Finally, there is an appendix.

## 2. SYSTEM MODEL

Consider a communication system consisting of a source node S, a full-duplex relay node R, a full-duplex destination node D, a passive eavesdropper node E, and a jammer node J, as shown in Figure 1 of this paper. Assume that S, E, and J each has a single antenna, while R and D are equipped with two antennas for transmission and reception. The relay R operates using the decode-and-forward (DF) protocol, D receives signals simultaneously from S and R, while node E only eavesdrops on the signal from R. Assume that node E cannot eavesdrop on the signal from node S due to terrain features such as trees, hills, high-rise buildings, etc., which obstruct the signal transmission path to node E. Given  $p \in \{S-R, S-E, R-D, R-E, D-R, D-E, J-E\}$ , the coefficient for the Rayleigh fading channel is  $h_p$  which is distributed according to  $h_p \sim CN(0, \lambda_p)$ , with  $\lambda_p = E\{|h_p|^2\}$  being

the average channel gain. By denoting  $q \in \{S, R, D, J\}$ , the transmit power at node  $q$  is  $P_q$ . The Gaussian noise at node  $k$  is  $n_k(t)$ , which follows the distribution  $n_k(t) \sim \mathcal{CN}(0, \sigma_k)$ , with the normalized noise variance being  $\sigma_k = N_0$ ,  $k \in \{R, D, E\}$ . The SNR at node  $k$  is denoted as  $\gamma_k$ . Since the channels in the system model follow the Rayleigh fading model, the probability density function (PDF) and the cumulative distribution function (CDF) of each channel gain are given by

$$f_{|h_p|^2}(x) = \frac{1}{\lambda_p} e^{-\frac{x}{\lambda_p}} \text{ and } F_{|h_p|^2}(x) = 1 - e^{-\frac{x}{\lambda_p}}, \text{ respectively, with } x > 0.$$

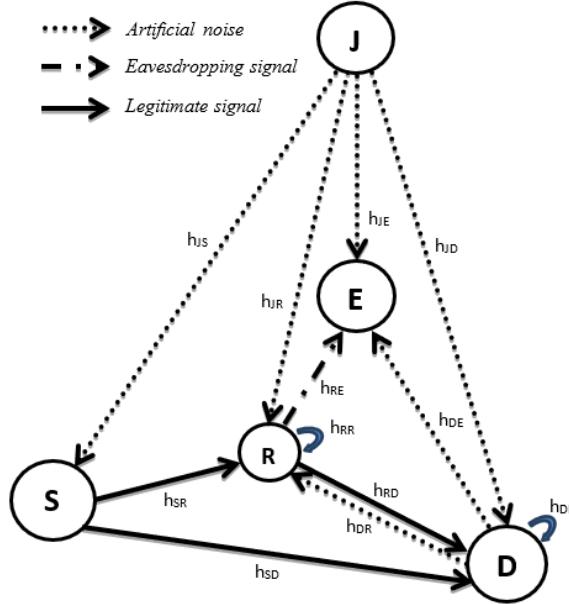


Figure 1. One-way full-duplex relay network model with the presence of an eavesdropping device.

Assume that at time  $t$ , S transmits signal  $x_S(t)$  to R and D. Meanwhile, D and J transmit a jamming signal  $w_D(t), w_J(t)$  to R and E, and E eavesdrops on the signal from R. The purpose of the jamming signals is to reduce the SNR at E, thereby enhancing the security performance.  $w_D(t), w_J(t)$  and  $x_S(t)$  are normalized such that  $E\{|w_D(t)|^2\} = E\{|w_J(t)|^2\} = E\{|x_S(t)|^2\} = 1$ , where  $E\{\cdot\}$  is the expectation operator. If R decodes  $x_S(t)$  successfully, it decodes and re-encodes before broadcasting. Otherwise, it keeps idle.

$$E\{|w_D(t)|^2\} = E\{|w_J(t)|^2\} = E\{|x_S(t)|^2\} = 1.$$

where  $E\{\cdot\}$  is the expectation operator.

At time  $t$ , the received signal at R is given as follows

$$y_R(t) = h_{SR}\sqrt{P_S}x_S(t) + h_{RR}\sqrt{P_R}x_R(t) + h_{DR}\sqrt{P_D}w_D(t) + h_{JR}\sqrt{P_J}w_J(t) + n_R(t) \quad (1)$$

Since the artificial noise can be known in advance at R [2-3], and R can cancel the interference  $h_{JR}w_J(t)$  and  $h_{DR}w_D(t)$ , the received signal after AN cancellation at R is given by

$$\tilde{y}_R(t) = h_{SR}\sqrt{P_S}x_S(t) + h_{RR}\sqrt{P_R}x_R(t) + n_R(t) \quad (2)$$

At time  $t$ , the received signals at E and D are given as follows

$$y_E(t) = h_{RE}\sqrt{P_R}x_R(t) + h_{DE}\sqrt{P_D}w_D(t) + h_{JE}\sqrt{P_J}w_J(t) + n_E(t) \quad (3)$$

$$y_D(t) = h_{SD}\sqrt{P_S}x_S(t) + h_{RD}\sqrt{P_R}x_R(t) + h_{DD}\sqrt{P_D}w_D(t) + h_{JD}\sqrt{P_J}w_J(t) + n_D(t) \quad (4)$$

Since the artificial noise can be known in advance at D, and D can cancel the interference  $h_{JD}w_J(t)$ , the received signal after AN cancellation at D is given by

$$\tilde{y}_D(t) = h_{SD}\sqrt{P_S}x_S(t) + h_{RD}\sqrt{P_R}x_R(t) + h_{DD}\sqrt{P_D}w_D(t) + n_D(t) \quad (5)$$

From (1), (3), and (4), the SNRs at the nodes R, E, and D at time  $t$  are respectively given as follows. The SNR at node R is

$$\gamma_R = \frac{|h_{SR}|^2 P_S}{|h_{RR}|^2 P_R + N_0} \quad (6)$$

The SNR at node E when R decodes  $x_S(t)$  successfully, which means  $x_R(t) = x_S(t)$ , is

$$\gamma_E = \frac{|h_{RE}|^2 P_R}{|h_{DE}|^2 P_D + |h_{JE}|^2 P_J + N_0} \quad (7)$$

The SNR at node E when R fails to decode  $x_S(t)$ , meaning  $x_R(t) \neq x_S(t)$ , is

$$\gamma_E^* = 0 \quad (8)$$

Then, the SNR at node D when R decodes  $x_S(t)$  successfully is

$$\tilde{\gamma}_D = \frac{|h_{SD}P_S + h_{RD}P_R|^2}{|h_{DD}|^2 P_D + N_0} \leq \gamma_D = \frac{|h_{SD}|^2 P_S + |h_{RD}|^2 P_R}{|h_{DD}|^2 P_D + N_0} \quad (9)$$

The SNR at node D when decoding  $x_S(t)$  fails:

The SNR at node D when R fails to decode  $x_S(t)$  is

$$\gamma_D^* = \frac{|h_{SD}|^2 P_S}{|h_{RD}|^2 P_R + |h_{DD}|^2 P_D + N_0} \quad (10)$$

### 3. SECURITY PERFORMANCE ANALYSIS

In this section, the SOP is derived. The secrecy capacity is defined as the difference between the legitimate channel capacity  $C_D$  and the eavesdropping channel capacity  $C_E$ :

$$C_S = [C_D - C_E]^+ = \frac{1}{2} \left[ \log_2 \frac{1 + \gamma_D}{1 + \gamma_E} \right]^+ \quad (11)$$

where  $C_T$  and  $C_E$  are the transmission signal capacity and the eavesdropping signal capacity, respectively,  $[x]^+ = \max(x, 0)$ .

**Theorem 1:** The CDF and PDF of  $\gamma_R$  are respectively given by

$$F_{\gamma_R}(x) = 1 - a_0 \frac{e^{-b_0 x}}{a_0 + x} \quad (12)$$

$$f_{\gamma_R}(x) = \frac{a_0 b_0 e^{-b_0 x}}{a_0 + x} + \frac{a_0 e^{-b_0 x}}{(a_0 + x)^2} \quad (13)$$

where  $a_0 = \frac{\lambda_{SR} P_S}{\lambda_{RR} P_R}$  and  $b_0 = \frac{N_0}{\lambda_{SR} P_S}$ .

*Proof of Theorem 1*

From (6), the CDF of  $\gamma_R$  is calculated as follows

$$\begin{aligned} F_{\gamma_R}(x) &= \Pr\left(\frac{|h_{SR}|^2 P_S}{|h_{RR}|^2 P_R + N_0} < x\right) \\ &= \Pr\left(x_0 < x \frac{(x_1 P_R + N_0)}{P_S}\right) \\ &= \int_0^{\infty} \left(1 - e^{-\frac{1}{\lambda_{SR}} x \frac{(x_1 P_R + N_0)}{P_S}}\right) \frac{1}{\lambda_{RR}} e^{-\frac{1}{\lambda_{RR}} x_1} dx_1 \\ &= 1 - a_0 \frac{e^{-b_0 x}}{a_0 + x} \end{aligned} \quad (14)$$

where  $x_0 = |h_{SR}|^2$  and  $x_1 = |h_{RR}|^2$ .

From (14), the PDF of  $\gamma_R$  is the first derivative of  $F_{\gamma_R}(x)$ , calculated as follows

$$f_{\gamma_R}(x) = -a_0 \frac{-b_0 e^{-b_0 x} (a_0 + x) - e^{-b_0 x}}{(a_0 + x)^2} = \frac{a_0 b_0 e^{-b_0 x}}{a_0 + x} + \frac{a_0 e^{-b_0 x}}{(a_0 + x)^2} \quad (15)$$

**Theorem 2:** The CDF of  $\gamma_D$  is given by

$$F_{\gamma_D}(y) = 1 - \frac{e^{-a_1 y}}{b_1(y + c_1)} \left(1 + \frac{1}{d_1}\right) + \frac{e^{-f_1 y}}{e_1 d_1(y + g_1)} \quad (16)$$

where  $a_1 = \frac{N_0}{\lambda_{RD} P_R}$ ,  $b_1 = \frac{\lambda_{DD} P_D}{\lambda_{RD} P_R}$ ,  $c_1 = \frac{\lambda_{RD} P_R}{\lambda_{DD} P_D}$ ,  $d_1 = \lambda_{RD} \left(\frac{P_R}{P_S \lambda_{SD}} - \frac{1}{\lambda_{RD}}\right)$ ,  $e_1 = \frac{\lambda_{DD} P_D}{P_S \lambda_{SD}}$ ,

$$f_1 = \frac{N_0}{P_S \lambda_{SD}}, \text{ and } g_1 = \frac{P_S \lambda_{SD}}{\lambda_{DD} P_D}.$$

*Proof of Theorem 2*

When R does successful decoding, one has

$$\begin{aligned} F_{\gamma_D}(y) &= \Pr\left(\frac{|h_{SD}|^2 P_S + |h_{RD}|^2 P_R}{|h_{DD}|^2 P_D + N_0} < y\right) \\ &= \Pr\left(\frac{Q}{|h_{DD}|^2 P_D + N_0} < y\right) \end{aligned} \quad (17)$$

where

$$\begin{aligned}
F_Q(q) &= \Pr(Q < q) \\
&= \Pr\left(\left|h_{SD}\right|^2 P_S + \left|h_{RD}\right|^2 P_R < q\right) \\
&= \int_0^{\frac{q}{P_R}} \left(1 - e^{-\frac{\frac{q}{P_R} - q_1 \frac{P_R}{P_S}}{\lambda_{SD}}}\right) \frac{1}{\lambda_{RD}} e^{-\frac{q_1}{\lambda_{RD}}} dq_1 \\
&= 1 - e^{-\frac{q}{\lambda_{RD} P_R}} - \frac{e^{-\frac{q}{\lambda_{RD} P_R}}}{\lambda_{RD} \left(\frac{P_R}{P_S \lambda_{SD}} - \frac{1}{\lambda_{RD}}\right)} + \frac{e^{-\frac{q}{P_S \lambda_{SD}}}}{\lambda_{RD} \left(\frac{P_R}{P_S \lambda_{SD}} - \frac{1}{\lambda_{RD}}\right)}
\end{aligned} \tag{18}$$

Therefore

$$\begin{aligned}
F_{\gamma_D}(y) &= \Pr(Q < y \left(\left|h_{DD}\right|^2 P_D + N_0\right)) \\
&= \int_0^{\infty} F_Q\left(y \left(y_0 P_D + N_0\right)\right) f_{\left|h_{DD}\right|^2}(y_0) dy_0 \\
&= 1 - \frac{e^{-a_1 y}}{b_1(y + c_1)} \left(1 + \frac{1}{d_1}\right) + \frac{e^{-f_1 y}}{e_1 d_1(y + g_1)}
\end{aligned} \tag{19}$$

where  $y_0 = \left|h_{DD}\right|^2$ .

When R suffers unsuccessful decoding, one has

$$\begin{aligned}
F_{\gamma_D^*}(z) &= \Pr\left(\frac{\left|h_{SD}\right|^2 P_S}{\left|h_{RD}\right|^2 P_R + \left|h_{DD}\right|^2 P_D + N_0} < z\right) \\
&= \Pr\left(z_0 < \frac{z}{P_S} (z_1 P_R + z_2 P_D + N_0)\right) \\
&= \int_0^{\infty} \int_0^{\infty} \left(1 - e^{-\frac{z}{\lambda_{SD} P_S} (z_1 P_R + z_2 P_D + N_0)}\right) f(z_1) f(z_2) dz_1 dz_2 \\
&= 1 - \frac{1}{a_3} \left( \frac{e^{-b_3 z}}{z + c_3} - \frac{e^{-b_3 z}}{z + d_3} \right)
\end{aligned} \tag{20}$$

where  $z_0 = \left|h_{SD}\right|^2$ ,  $z_1 = \left|h_{RD}\right|^2$  and  $z_2 = \left|h_{DD}\right|^2$ .

**Theorem 3:** The CDF and PDF of  $\gamma_E$  are respectively given by

$$F_{\gamma_E}(t) = 1 - \frac{1}{b_2} \left( \frac{e^{-a_2 t}}{(t + c_2)} - \frac{e^{-a_2 t}}{(t + d_2)} \right) \tag{21}$$

and

$$f_{\gamma_E}(t) = \frac{1}{b_2} \left( \frac{a_2 e^{-a_2 t}}{(t + c_2)} + \frac{e^{-a_2 t}}{(t + c_2)^2} - \frac{a_2 e^{-a_2 t}}{(t + d_2)} - \frac{e^{-a_2 t}}{(t + d_2)^2} \right) \quad (22)$$

where  $a_2 = \frac{N_0}{\lambda_{RE} P_R}$ ,  $b_2 = \frac{\lambda_{DE} P_D}{\lambda_{RE} P_R} - \frac{\lambda_{JE} P_J}{\lambda_{RE} P_R}$ ,  $c_2 = \frac{\lambda_{RE} P_R}{\lambda_{DE} P_D}$ , and  $d_2 = \frac{\lambda_{RE} P_R}{\lambda_{JE} P_J}$ .

*Proof of Theorem 3*

Analyzing (7), we have the CDF of  $\gamma_E$  by applying [18, eq. (3.352.4) and eq. (3.353.3)]

$$\begin{aligned} F_{\gamma_E}(t) &= \Pr \left( \frac{|h_{RE}|^2 P_R}{|h_{DE}|^2 P_D + |h_{JE}|^2 P_J + N_0} < t \right) \\ &= \int_0^\infty \int_0^\infty \left( 1 - e^{-\frac{t}{\lambda_{RE} P_R} (t_1 P_D + t_2 P_J + N_0)} \right) f(t_1) f(t_2) dt_1 dt_2 \\ &= 1 - \frac{1}{b_2} \left( \frac{e^{-a_2 t}}{t + c_2} - \frac{e^{-a_2 t}}{t + d_2} \right) \end{aligned} \quad (23)$$

where  $t_1 = |h_{DE}|^2$  and  $t_2 = |h_{JE}|^2$ .

From (23), the PDF of  $\gamma_E$  is the first derivative of  $F_{\gamma_E}(t)$ , calculated as follows

$$f_{\gamma_E}(t) = \frac{1}{b_2} \left( \frac{a_2 e^{-a_2 t}}{t + c_2} + \frac{e^{-a_2 t}}{(t + c_2)^2} - \frac{a_2 e^{-a_2 t}}{t + d_2} - \frac{e^{-a_2 t}}{(t + d_2)^2} \right) \quad (24)$$

### 3.1. System secrecy outage probability

The SOP is the probability that occurs if the secrecy capacity is lower than a given threshold  $C_{th}$ , hence given by

$$SOP = \Pr(C_S < C_{th}) \quad (25)$$

where  $C_S$  is the secure capacity of the system, and  $C_{th}$  is the predefined threshold of the capacity at the legitimate eavesdropper node.

When the node R does successful decoding, the SOP is calculated as follows

$$\begin{aligned} SOP_{\text{Nerror}} &= \Pr(C_s^{\text{Nerror}} < C_{th}) \\ &= \Pr \left( \log_2 \frac{1 + \gamma_D}{1 + \gamma_E} < C_{th} \right) \\ &= \Pr \left( \gamma_D < 2^{C_{th}} \gamma_E + 2^{C_{th}} - 1 \right) \\ &= F_{\gamma_D} \left( 2^{C_{th}} \gamma_E + 2^{C_{th}} - 1 \right) \end{aligned} \quad (26)$$

When the node R suffers unsuccessful decoding, the SOP is calculated as follows

$$\begin{aligned}
SOP_{Error} &= \Pr(C_S^{Error} < C_{th}) \\
&= \Pr\left(\log_2 \frac{1+\gamma_D^*}{1+\gamma_E^*} < C_{th}\right) \\
&= \Pr(\gamma_D^* < 2^{C_{th}} \gamma_E^* + 2^{C_{th}} - 1) \\
&= \Pr(\gamma_D^* < 2^{C_{th}} - 1) \\
&= F_{\gamma_D^*}(2^{C_{th}} - 1)
\end{aligned} \tag{27}$$

Therefore, the SOP of the system is provided by

$$\begin{aligned}
SOP &= SOP_{Nerror} \Pr(\gamma_R \geq 2^{C_{th}} - 1) + SOP_{Error} \Pr(\gamma_R < 2^{C_{th}} - 1) \\
&= SOP_{Nerror} (1 - \Pr(\gamma_R < 2^{C_{th}} - 1)) + SOP_{Error} \Pr(\gamma_R < 2^{C_{th}} - 1) \\
&= SOP_{Nerror} (1 - F_{\gamma_R}(2^{C_{th}} - 1)) + SOP_{Error} F_{\gamma_R}(2^{C_{th}} - 1)
\end{aligned} \tag{28}$$

### 3.2. Secrecy throughput

The secrecy throughput is the product of the secrecy rate and the secrecy outage probability, defined as follows

$$STP = R_s(1 - SOP) \text{ (bit/s/Hz)} \tag{29}$$

where  $STP$  is the secrecy throughput of the system,  $R_s$  is the secrecy rate of the system, and  $SOP$  is the secrecy outage probability of the system.

## 4. RESULTS AND DISCUSSION

This section presents numerical results and simulations to verify the proposed SOP and STP expressions, and evaluate the security performance of the OWFD relay network. The SOP and STP are evaluated based on key operating parameters, such as the position of R, the position of E, the path loss exponent  $\beta$ , the given threshold of the capacity  $C_{th} = \{0.01, 0.05, 0.1\}$  (bits/s/Hz).

To illustrate the performance, the coordinates of the users are chosen as  $S$  at  $(0.0, 0.0)$ ,  $D$  at  $(8.0, 8.0)$ ,  $R$  at  $(5.0, 4.0)$ ,  $E$  at  $(10.0, 14.0)$ ,  $J$  at  $(8.0, 20.0)$ . In the following,  $x_S, x_D, x_E, x_J$  and  $y_S, y_D, y_E, y_J$  represent the x-coordinate and y-coordinate of  $S, D, E, J$ , respectively. Additionally,  $P_S = 20$  dB,  $P_R = 1$  dB,  $P_D = -25$  dB and  $P_J = 25$  dB are considered. The path loss and fading power are modeled as  $d^{-\beta}$ , with  $d$  representing the distance from the transmitter to the receiver. Among all the results, one result considers different transmission environments, so the value of  $\beta$  is selected to run from 1 to 6, while the remaining results are chosen with  $\beta = 3$ .

Figure 2 describes the effect of SNR on  $SOP$  at three different positions of node  $J$  with  $y_D = \{20, 25, 30\}$  meters and  $C_{th} = 0.01$  (bits/s/Hz). This figure shows the match between the simulation and analysis, validating the proposed  $SOP$  expressions. It can be observed that as  $P_S/\sigma^2$  increases,  $SOP$  decreases. This can be explained as follows: Node  $E$  eavesdrops on the signal from nodes  $S, R, D$  while being affected by AN from node  $J$ , whereas node  $D$  only receives the signal from node  $R$  and cancels out the AN from node  $J$ . Therefore, as  $P_S/\sigma^2$  increases, the SNR at  $E$

increases, but at a slower rate than the SNR at  $D$ , because node  $E$  receives three channels. There are two channels with noise, so these noise components reduce the increase of SNR at  $E$ , which causes  $C_S$  to increase, and thus  $SOP$  decreases. Additionally, as node  $J$  moves further away from the four nodes  $S, R, D, E$ , the SNR at  $E$  increases, leading to a decrease in  $C_S$ , while the SNR at  $D$  remains constant, causing  $SOP$  to increase.

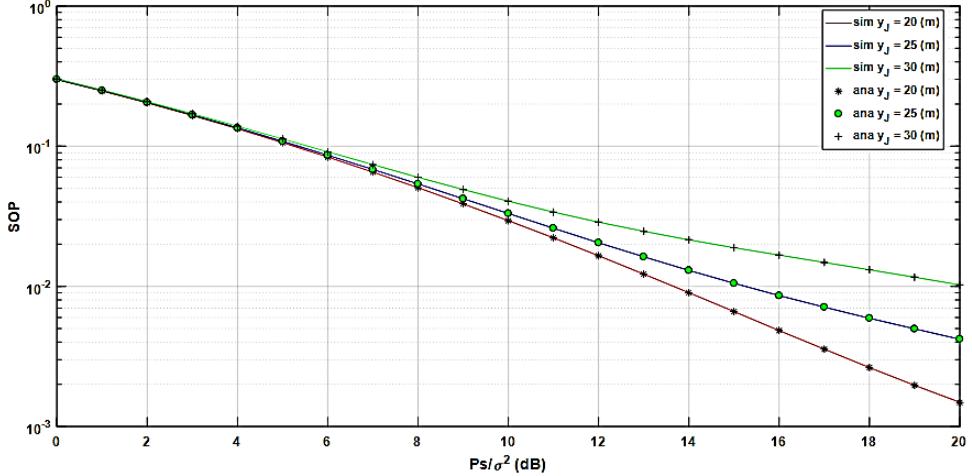


Figure 2. The effect of SNR on  $SOP$  at three different positions of node  $J$ .

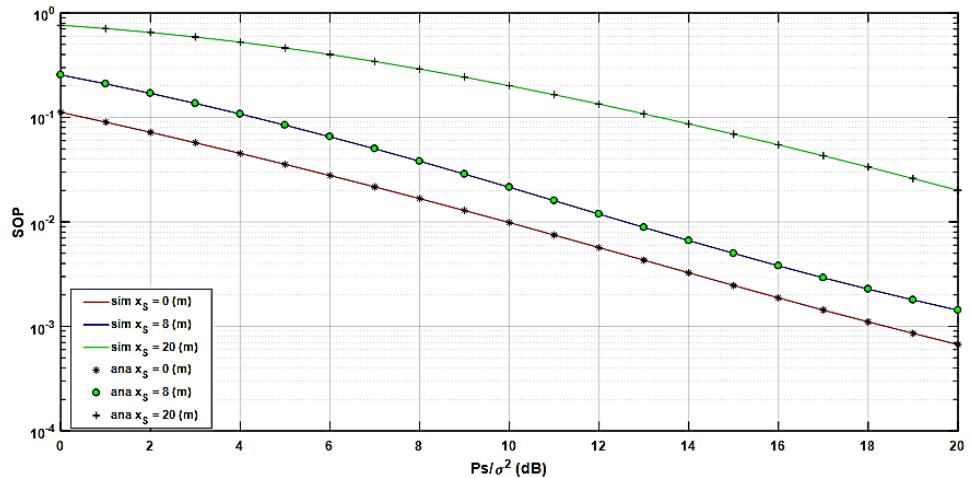


Figure 3. The impact of value  $P_S/\sigma^2$  when changing the position of node  $S$ .

Figure 3 illustrates the effect of the distance of node  $S$  on  $SOP$  as different values of  $P_S/\sigma^2$  are varied. The graph shows the match between simulation and analysis. As the transmission power of node  $S$ ,  $P_S/\sigma^2$  increases, the SNR at node  $R$  and  $D$  increases, leading to an increase in the system's security, or in other words,  $SOP$  decreases. Since the SNR at node  $D$  increases, the system's secrecy capacity increases, causing  $SOP$  to decrease. On the other hand, as the x-coordinate of node  $S$  increases, the SNR at  $D$  decreases, causing  $SOP$  to increase.

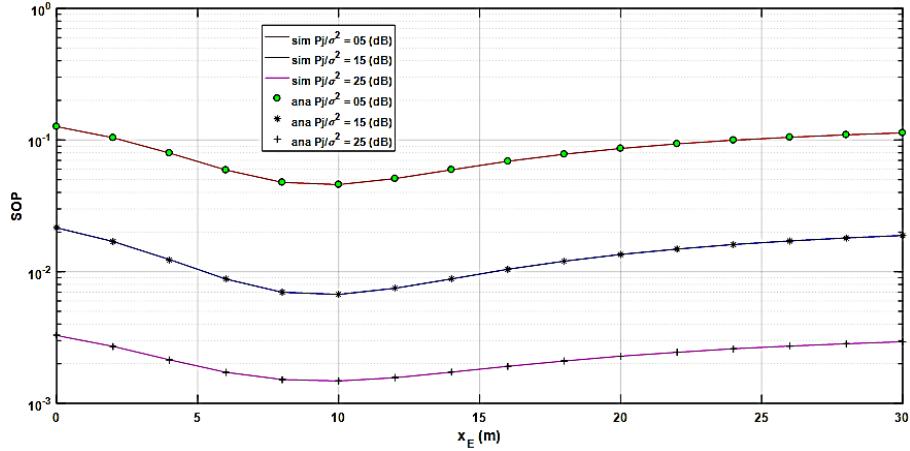


Figure 4. The effect of the position of node E on  $SOP$  as the value of  $P_S/\sigma^2$  changes.

Figure 4 illustrates the effect of the distance of node E on  $SOP$  at three different values of  $P_S/\sigma^2$ . The graph shows the match between simulation and analysis. As the value of  $x_E$  gets closer to node J,  $SOP$  decreases, and as it moves further away from node J,  $SOP$  increases. This can be explained as follows: The node E is closer to node J, the higher the noise power at node E, and vice versa. Therefore, the SNR at node E increases, leading to a decrease in  $SOP$ , and vice versa. Furthermore, the adjacent position  $x_E = 8$  (m) of node E results in a minimum  $SOP$ , as it is closest to nodes D and J, causing the SNR at node E to be the lowest. On the other hand, as the transmission power of node J increases,  $SOP$  decreases because the SNR at node D increases, which in turn leads to an increase in the system's secrecy capacity.

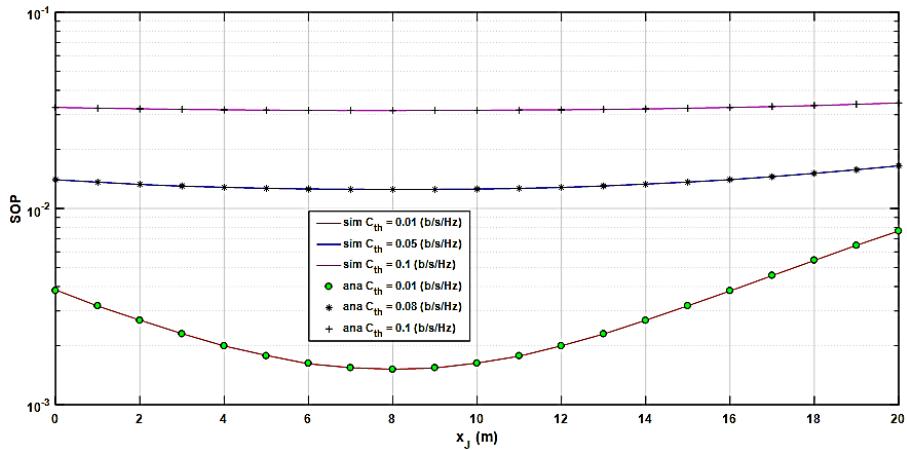


Figure 5. The effect of  $x_J$  on  $SOP$  at three different values of  $C_{th}$ .

Figure 5 shows the match between simulation and analysis. This figure illustrates that as the length  $x_J$  increases up to 8 (m),  $SOP$  gradually decreases. Beyond 8 (m),  $SOP$  starts to increase because, at  $x_J = 8$  (m), node J is closest to node E, while the distance from node E to node D remains fixed. As a result, the SNR at E is the lowest, meaning it reaches a minimum at point  $J = (8.0, 20.0)$ , leading to a minimum  $SOP$ . At the same time, the higher the predefined threshold  $C_{th}$ , the greater the  $SOP$  of the system.

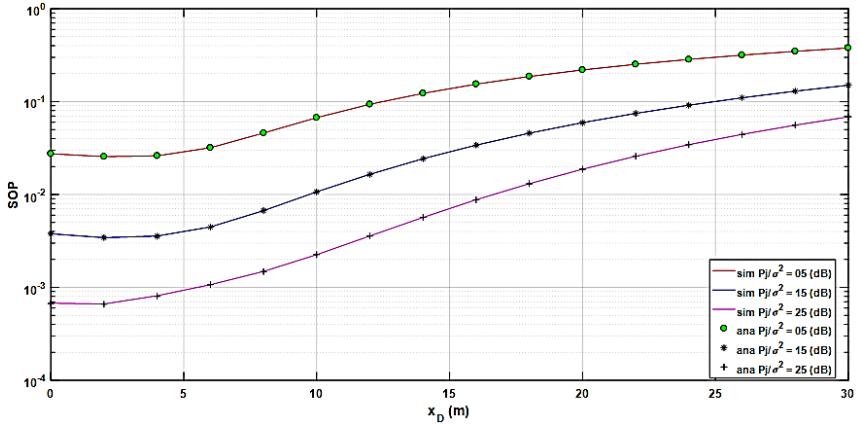


Figure 6. The impact of  $x_D$  on SOP at three values of  $P_J/\sigma^2$ .

Figure 6 illustrates the impact of the distance of node D on  $SOP$  when varying the values of  $P_J/\sigma^2$ . The graph shows a match between simulation and analysis. As the transmit power of node D, denoted as  $P_D/\sigma^2$ , increases, the SNR at node E decreases, leading to a reduction in system security; in other words,  $SOP$  increases. On the other hand, as the abscissa of node  $x_D$  increases, meaning the distance from node D to node E increases, the SNR at E decreases, causing  $SOP$  to increase. Furthermore, when the distance between nodes is fix and the transmit power  $P_J/\sigma^2$  increases, the SNR at node E decreases, resulting in a decrease in SOP.

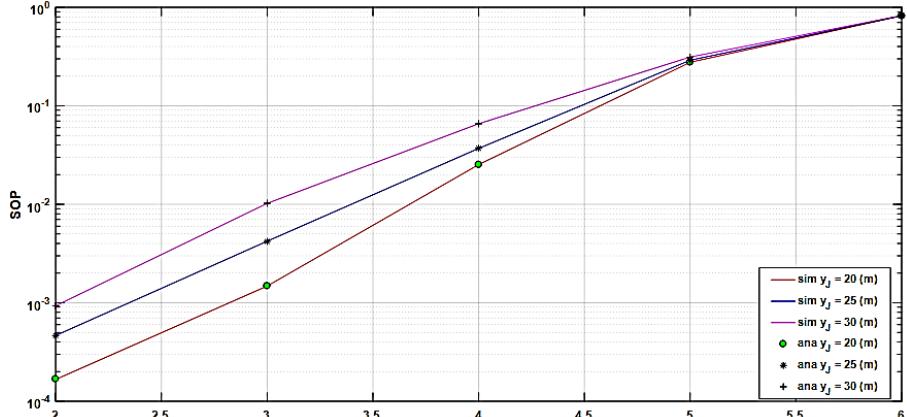


Figure 7. The effect of  $\beta$  on SOP at three values of  $y_J = \{20, 25, 30\}$  (m).

Figure 7 illustrates the effect of  $\beta$  on  $SOP$  and also shows the match between simulation and analysis. It is clearly observed that as  $\beta$  increases, the received noise power at node E increases, leading to a decrease in SNR at node E. As a result,  $C_S$  increases, causing  $SOP$  to decrease. The simulation results clearly show that at  $\beta=2$ ,  $SOP$  reaches its minimum. On the other hand, as node J moves further away from node E, the SNR at node E decreases, leading to an increase in  $SOP$  of the system.

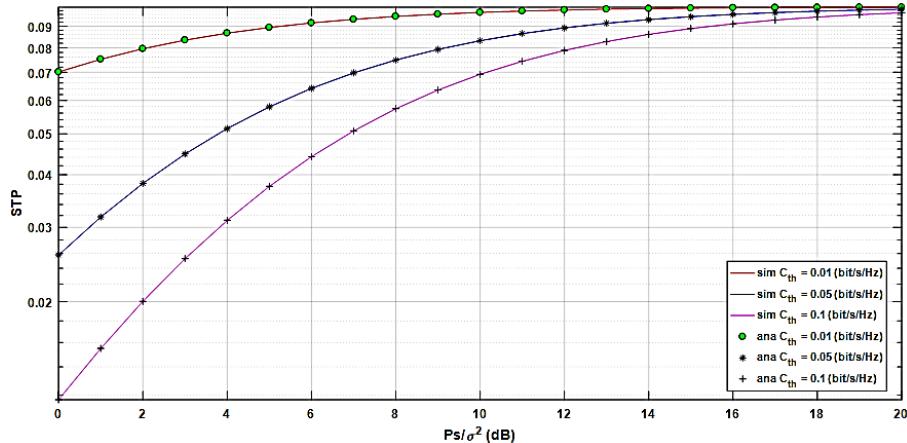


Figure 8. The influence of  $P_S/\sigma^2$  on STP at three Values of  $C_{th}$ .

Figure 8 illustrates the impact of  $P_S/\sigma^2$  on STP, also showing the consistency between simulation and analysis. It can be observed that as  $P_S/\sigma^2$  increases,  $C_S$  also increases because the throughput is inversely proportional to the system's secure stopping probability. As a result,  $SOP$  decreases, leading to an increase in STP. On the other hand, as node E moves closer to node J while node D remains fixed,  $C_S$  increases because the SNR at node E decreases. As a result,  $SOP$  decreases, leading to an increase in STP. Therefore,  $P_S/\sigma^2$  is always directly proportional to STP and inversely proportional to  $SOP$ .

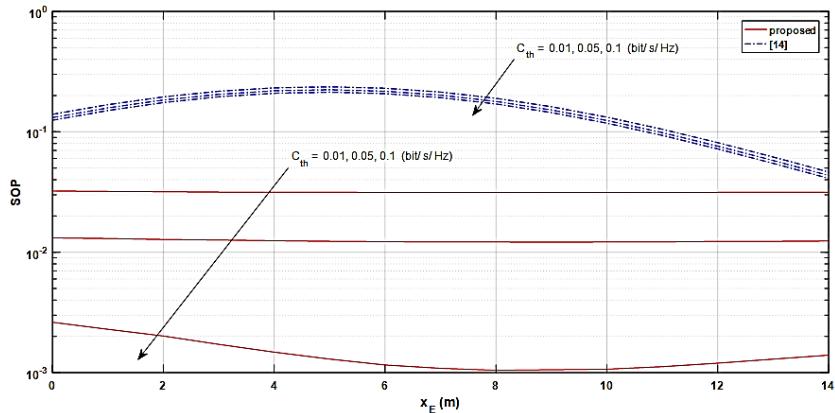


Figure 9. Comparison of  $SOP$  between the proposed model and [14] when varying  $C_{th}$ .

Figure 9 illustrates the simulation curves comparing the proposed model with the reference model in [14]. For a fair comparison, the total transmission power in both models is set to be equal. The results show that the SOP of the proposed model is significantly lower than that of the reference model. In other words, the security performance of the proposed model is much better than that of the reference model [14].

## 5. CONCLUSION

The problem model has proposed a jamming protocol to generate AN for the OWFD system. The AN is transmitted from J and D to reduce the signal capacity received by E, thereby increasing reliability R and improving  $C_S$  of the system. The analysis clearly showed that jamming is significantly more effective than non-jamming for the system. The results also indicated that the higher the SNR, the lower

the SOP of the system, which leads to a higher STP of the system. By using MATLAB software and the Monte Carlo simulation method, the accuracy of analyzing the problems in the system is demonstrated through the alignment between the simulation curve and the analytical curve. Additionally, the results have assessed the impact of parameter  $\beta$  on the SOP of the system.

The paper has proposed the OWFD relay networks with AN. The analysis clearly showed that introducing AN is always much more effective than not introducing it into the system model. The results also indicated that as the SNR increases, the SOP decreases, leading to a higher STP. By using the MATLAB software and the Monte Carlo simulation method, the accuracy of the analysis has been demonstrated through the alignment between the simulation curve and the analytical curve. Furthermore, the results have provided the optimal selection of the power division coefficient and capacity threshold for maximum security performance. The results also evaluated how  $\beta$  influences security performance.

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## TÓM TẮT

### DÁNH GIÁ HIỆU NĂNG BẢO MẬT CHO MẠNG CHUYỀN TIẾP SONG CÔNG MỘT CHIỀU SỬ DỤNG NHIỀU NHÂN TẠO

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Bài báo này trình bày phương pháp để cải thiện các vấn đề bảo mật lớp vật lý (PLS) trong mạng truyền thông không dây. Cụ thể, chúng tôi xem xét mô hình mạng chuyển tiếp song công một chiều (OWFD) có gây nhiễu nhân tạo (AN) và sử dụng kênh truyền Rayleigh fading. Mô hình bao gồm năm nút: nút nguồn, nút chuyển tiếp, nút nghe lén, nút đích và nút gây nhiễu. Để đánh giá hiệu năng bảo mật của mô hình, chúng tôi tiến hành phân tích các thông số của các yếu tố như: xác suất dùng bảo mật (SOP), thông lượng bảo mật (STP) của hệ thống. Chúng tôi cũng đã đưa ra được các công thức dạng đóng cho các thông số SOP, STP trong mô hình. Kiểm chứng cho kết quả mô phỏng với kết quả tính toán bằng phương pháp Monte-Carlo. Kết quả nghiên cứu của bài báo cho thấy hiệu năng bảo mật được cải thiện đáng kể so với những nghiên cứu trước đây, đồng thời, mô hình để xuất cũng cho thấy tính khả thi của việc triển khai các vấn đề PLS trong mạng OWFD.

*Từ khóa:* Bảo mật lớp vật lý, Xác suất dùng bảo mật, Thông lượng bảo mật, Nhiều nhân tạo, Song công một chiều.